

SPRING 2003 Midterm Exam #3, Part A

Exam time limit: 50 minutes. You may use calculators and both sides of 2 pages of notes, handwritten only. Closed book; no collaboration. For multiple choice questions, circle the one best answer or letter (unless more than one answer is asked for).

Some moments of inertia:

hoop or thin ring: $I = M R^2$	thin rod, about center: $I = (1/12) M L^2$
solid cylinder or disk: $I = (1/2) M R^2$	thin rod, about end: $I = (1/3) M L^2$
solid sphere: $I = (2/5) M R^2$	

(1 pt. each, unless otherwise specified)

1. (2 pts.) A 5.0-kg mass traveling with velocity 10. cm/s to the right collides head-on with a 2.0-kg mass traveling with velocity v_2 to the left. They stick together in the collision. In order for the stuck-together pair to have *zero velocity* after the collision, the **speed** v_2 must equal:

- | | |
|-------------|-------------|
| A. zero | D. 6.0 cm/s |
| B. 4.0 cm/s | E. 10. cm/s |
| C. 5.0 cm/s | F. 25 cm/s |

2. A spaceship with total mass M is drifting through space at a constant velocity V .

a. If the spaceship suddenly explodes, the **sum of the momenta** of all the little pieces is...

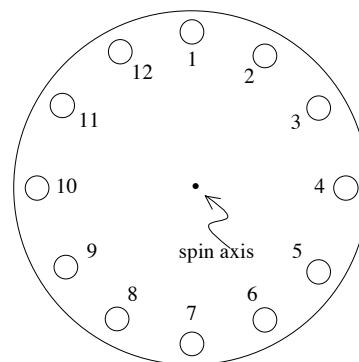
- | | |
|-------------------|----------------------|
| A. zero | C. equal to MV |
| B. less than MV | D. greater than MV |

b. The **sum of the KE** of all the little pieces is... (*Hint: The answer is the same as in the special case of $V = 0$.*)

- | | |
|--------------------------|-----------------------------|
| A. zero | C. equal to $(1/2)MV^2$ |
| B. less than $(1/2)MV^2$ | D. greater than $(1/2)MV^2$ |

3. (2 pts.) A centrifuge is designed to hold and spin as many as 12 test tubes simultaneously. It has evenly-spaced holders labeled #1 through #12, as shown. The centrifuge is properly "balanced" only when the *center of mass* of all of its contents is located exactly on the spin axis of the centrifuge. Which **two** of the following test tube configurations are **NOT** balanced?

- | | |
|---------------|---------------------------------|
| A. #1 only | D. #1, #2, #7, #8 |
| B. #1 and #7 | E. #1, #3, #7, #11 |
| C. #1, #5, #9 | F. all filled except #4 and #10 |



4. A tightrope walker carries a long sideways pole to aid in balance. She can choose between two poles to use: both with the *same* mass, but one with *twice* the length of the other. She should choose the **longer** pole because...

- | | |
|--|---|
| A. it has the greater angular velocity | C. it has the greater weight |
| B. it has the greater angular acceleration | D. it has the greater moment of inertia |

5. A child ($m = 30$ kg) is riding on the edge on a merry-go-round ($M = 300$ kg) spinning at angular speed ω . (Assume there is no air resistance or frictional torque acting on the system.) As the child slowly moves from the edge of the merry-go-round toward the center, which **one** of the following happens to the child+merry-go-round system?

- | | |
|-----------------------|------------------|
| A. ω increases | C. L increases |
| B. I increases | D. T increases |

6. a. A standard “LP” music record spins at 33 rpm (revolutions per minute). What is its **angular speed**, ω ?

- A. 0.030 rad/s
- B. 0.29 rad/s
- C. 0.55 rad/s
- D. 1.8 rad/s
- E. 3.5 rad/s
- F. 21 rad/s

b. (2 pts.) If a record player is accelerated from rest up to full speed at $\alpha = 1.4 \text{ rad/s}^2$, how many **revolutions** does it complete during this time?

- A. 0.20 rev
- B. 0.68 rev
- C. 1.7 rev
- D. 3.2 rev
- E. 6.3 rev
- F. 8.6 rev

c. (2 pts.) The turntable itself has a mass of 0.30 kg, radius of 15 cm, and a thickness of 3.0 mm. How much **torque** must the motor provide to accomplish the acceleration in part (b)?

- A. zero
- B. $2.3 \times 10^{-3} \text{ m}\cdot\text{N}$
- C. $3.0 \times 10^{-3} \text{ m}\cdot\text{N}$
- D. $4.7 \times 10^{-3} \text{ m}\cdot\text{N}$
- E. $5.8 \times 10^{-3} \text{ m}\cdot\text{N}$
- F. $1.6 \times 10^{-2} \text{ m}\cdot\text{N}$

d. Once the turntable reaches full speed, how much **torque** must the motor provide to keep it at a *constant* 33 rpm?

- A. zero
- B. $2.3 \times 10^{-3} \text{ m}\cdot\text{N}$
- C. $3.0 \times 10^{-3} \text{ m}\cdot\text{N}$
- D. $4.7 \times 10^{-3} \text{ m}\cdot\text{N}$
- E. $5.8 \times 10^{-3} \text{ m}\cdot\text{N}$
- F. $1.6 \times 10^{-2} \text{ m}\cdot\text{N}$

7. A baton twirler is moving with a constant horizontal speed v when she throws her spinning baton high into the air. (A baton is basically a lightweight rod with a mass fixed to each end.) Ignoring air resistance, which **one** of the following is TRUE?

- A. A baton will always spin about the rod’s center, even if the masses on its two ends are different.
- B. The baton will spin slowest at the very top of its arc, and fastest when it is closest to the ground.
- C. The total KE of the baton is least at the very top of its arc, and greatest when it is closest to the ground.
- D. The baton’s center of mass moves with a complicated, loopy path through the air.

8. (2 pts.) A simple lever gives the user a mechanical advantage: pushing down with force F on the long end of the lever creates an upward force greater than F on the short end. If you want to (just barely) lift mass m using a lever of length L , and the fulcrum is located at a distance of exactly $L/7$ from the short end of the lever, with what **force** F must you push down on the long end?

- A. $(1/7) mg$
- B. $(1/6) mg$
- C. $(1/\sqrt{7}) mg$
- D. $(1/\sqrt{6}) mg$
- E. $(5/6) mg$
- F. $(6/7) mg$



9. The three great Conservation Laws we have encountered are:

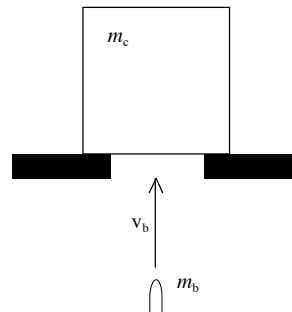
- A. Energy, Work, and Force
- B. Momentum, Impulse, and Energy
- C. Torque, Force, and Power
- D. Inertia, Mass, and Energy
- E. Momentum, Angular Momentum, and Energy
- F. Kinetic Energy, Potential Energy, and Work done by non-conservative forces

SPRING 2003 Midterm Exam #3, Part B

Exam time limit: 50 minutes. You may use calculators and both sides of 2 pages of notes, *handwritten only*. Closed book; no collaboration. Show your work on free-response questions. Be sure to use **proper units** and **significant figures** in your final answers.

1. A bullet (mass $m_b = 15.6$ g) is fired directly upward into a wooden cube ($m_c = 4.50$ kg), where it lodges in the wood. The cube then flies up into the air to a maximum height h above its starting position.

a. (4 pts.) If the bullet has a velocity $v_b = 426$ m/s immediately before impact, and the cube starts at rest, what is the **velocity** of the bullet+cube immediately after impact? Show your work.



b. (1 pt.) Which one of the following is TRUE?

- A. The collision is elastic because momentum is lost in the collision.
- B. The collision is elastic because KE is lost in the collision.
- C. The collision is elastic because momentum & KE are both lost in the collision.
- D. The collision is inelastic because momentum is lost in the collision.
- E. The collision is inelastic because KE is lost in the collision.
- F. The collision is inelastic because momentum & KE are both lost in the collision.

c. (3 pts.) Find the **maximum height h** of the bullet+cube. Show your work.

2. A bowling ball (a uniform sphere with $R = 10.8$ cm and $M = 7.25$ kg) rolls at 5.00 m/s without slipping on a horizontal surface.

a. (5 pts.) Calculate the **TOTAL kinetic energy** of the bowling ball.

(2. cont'd.) b. (3 pts.) The bowling ball then encounters an incline. To what **height** will it roll before stopping? Show your work.

c. (1 pt.) You repeat the above experiment using a *hollow cylinder* (same M and R as the bowling ball) rolling at 5.00 m/s without slipping, and then using a *block of ice* (same M) sliding frictionlessly at 5.00 m/s. **Choose one:**

- A. The bowling ball reaches the greatest height on the incline, and the block of ice the least.
- B. The bowling ball reaches the greatest height on the incline, and the hollow cylinder the least.
- C. The hollow cylinder reaches the greatest height on the incline, and the block of ice the least.
- D. The block of ice reaches the greatest height on the incline, and the bowling ball the least.
- E. The block of ice reaches the greatest height on the incline, and the hollow cylinder the least.
- F. All three reach the same height on the incline.

3. (5 pts.) A heavy wood beam with length L and mass m is fixed to a wall at point P , and also suspended by a steel cable at angle α . (The mass of the cable is negligible.) Find the magnitude of the **force of tension** F_T in the cable, in terms of the variables m , L , α , and g .

(Hint: Sum the torques acting on the beam, using point P as the pivot. You will NOT also need to sum the forces acting on the beam. Not all of the variables will necessarily appear in your answer.)

