Physics 272. Midterm I

Please write your name at the top of the page There are 4 problems. Each is assigned 25 points. Show your work.

Problem 1: 25 points

Three point charges are placed on the x-axis. $q_1=-6.0\mu\mathrm{C}$ is at x=-3.0 m, $q_2=4.0\mu\mathrm{C}$ is at the origin and $q_3=-6.0\mu\mathrm{C}$ is at x=3.0 m. (Useful constant: $k=8.99\times10^9~\mathrm{N/m^2C^2}$)

- (a) Find the **magnitude** of the *force* on q_1 .
- (b) What is the **magnitude** of the *electric field* at the position of q_1 . ?
- (c) What is the direction of the *electric field* at the position of q_1 . ?

Problem 2: 25 points

An infinitely long cylinder of radius R carries a uniform volume charge density $\rho(r) = \rho_0$.

- (a) Find the magnitude of the electric field inside the cylinder as a function of radius. (draw a diagram which shows the Gaussian surface used.)
- (b) Find the magnitude of the electric field outside the cylinder as a function of radius.
- (c) What is the **direction** of the electric field? (show it on your diagram)

Problem 3: 25 points

Two concentric spherical shell conductors carry equal and opposite charges. The inner shell has radius a and charge q; the outer shell has radius b and charge -q.

- (a) Draw a sketch of this configuration.
- (b) Find the *potential difference* between the two shells (i.e. $V_a V_b$). (your answer should be given in terms of a, b and q.)
- (c) Find the *capacitance* of this arrangement. (your answer should be given in terms of a, b and q.)

Problem 4: 25 points

- (a) Half the charge is removed from a capacitor without changing the capacitance. What fraction of its stored energy is removed along with the charge?
- (b) Two charged metal spheres are connected by a conducting wire and sphere A is larger than sphere B, is the magnitude of the electric potential of sphere A (larger, smaller, or the same) as that of sphere B? Explain.
- (c) Two metal balls have charge +q and -q. How will the *force* on them change if the balls are placed in water, the distance between them being unchanged?
- (d) Three charges +q, +Q, -q are placed at the corners of an equilateral triangle as shown. What is the direction of the net force on charge +q?

(e) A dielectric with dielectric constant $\kappa = 3.0$ is inserted between the plates of a parallel plate capacitor, by what factor does the *potential difference* and capacitance change?