

Course Updates

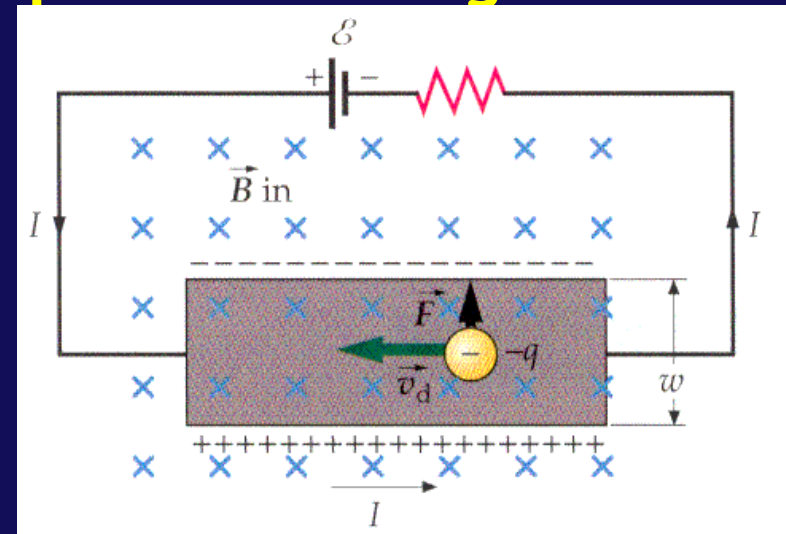
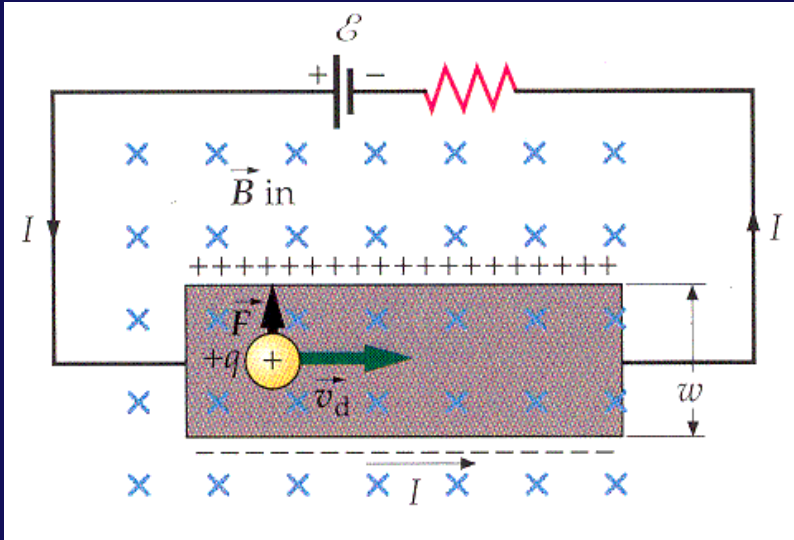
<http://www.phys.hawaii.edu/~varner/PHYS272-Spr10/physics272.html>

Reminders:

- 1) HW # 7 due today
- 2) Assignment #8 available
- 3) Chapter 28 this week

The Hall Effect

- Is current due to motion of positive or negative



- Positive charges moving *CCW* experience upward force
- Upper plate at *higher* potential
- Negative charges moving clockwise experience upward force
- Upper plate at *lower* potential

Equilibrium between electrostatic & magnetic forces:

$$F_{\text{up}} = qv_{\text{drift}}B \quad F_{\text{down}} = qE_{\text{induced}} = q\frac{V_H}{w} \quad V_H = v_{\text{drift}}Bw = \text{"Hall Voltage"}$$

- This type of experiment led to the discovery (E. Hall, 1879) that current in conductors is carried by negative charges (not always so in semiconductors).
- Can be used as a B-sensor.

Example

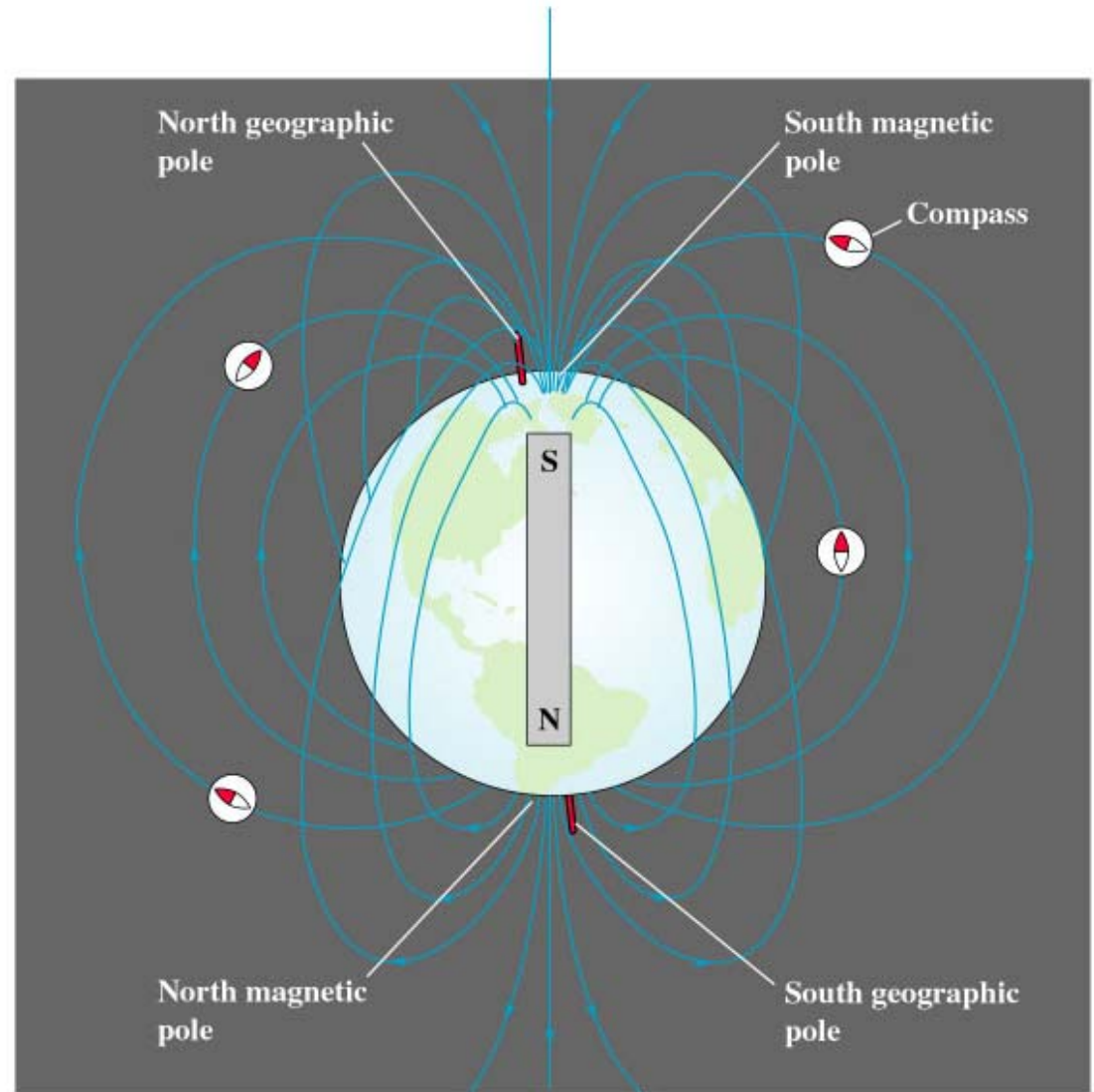
Flight over North Pole

$$V_H = v_{\text{drift}} B w = \text{"Hall Voltage"}$$

$$600 \text{ mi/hr} = 268 \text{ m/s}$$

$$B \text{ vertical} \sim 0.5 \times 10^{-4} \text{ T}$$

$$\text{Wingspan} \sim 30 \text{ m}$$



Sources of Magnetic Fields (chap 28)

In Chapter 27, we considered the magnetic field effects on a moving charge, a line current and a current loop.

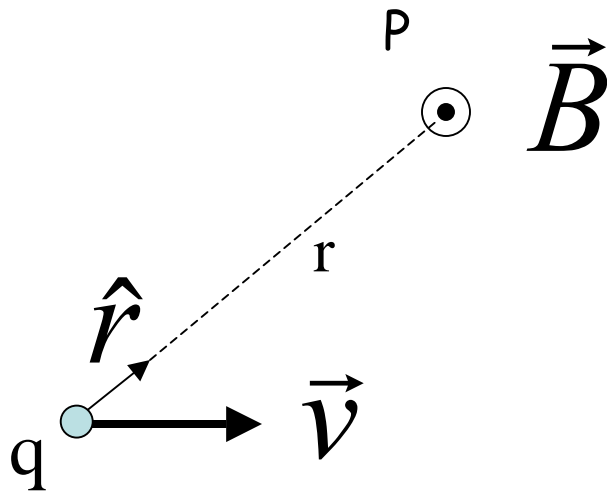
Now in Chap 28, we consider the magnetic fields that are created by:

- moving charges
- line current elements (Biot-Savart Law)
- line of current
- current loops

Magnetic Fields from a moving charge

Magnetic fields are created by a moving charge. If the charge is stationary, there is NO magnetic field. If the charge is moving, the magnetic field law is

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \hat{r}}{r^2}$$



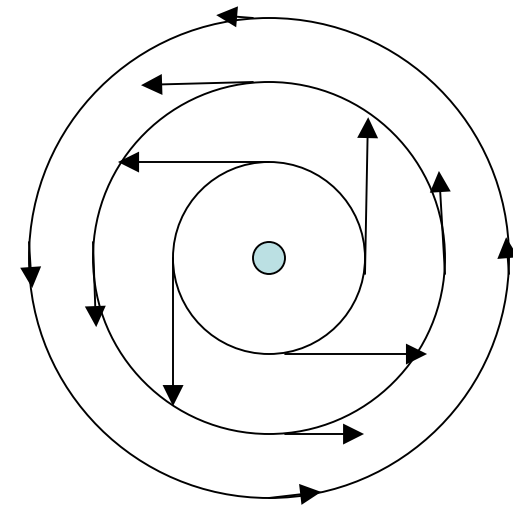
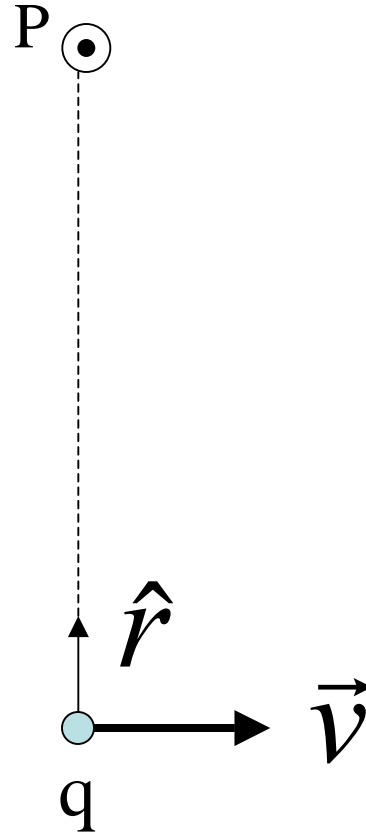
$$\mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m} / \text{A}$$

Use right hand to get
direction of field

Magnetic Fields from a moving charge at a position perpendicular to velocity

$$\sin \theta = 1$$

$$|\vec{B}| = \frac{\mu_0}{4\pi} q |\vec{v}| \frac{1}{r^2}$$

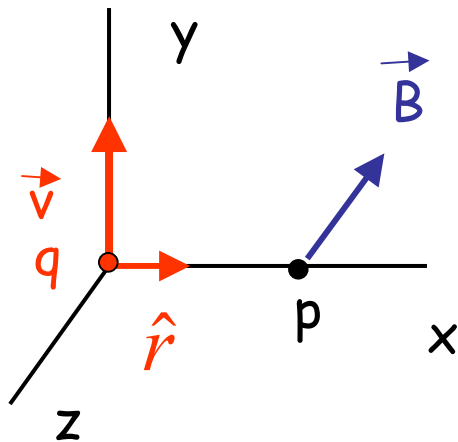


v is out of screen.
B field lines have
circular path.

Example

A $q=6\mu\text{C}$ point charge at the origin is moving with a $v=8\times 10^6\text{m/s}$ in the $+y$ direction. What is the B field it produces at the following points?

A) $x=0.5\text{m}, y=0, z=0$



$$\begin{aligned}\vec{B} &= \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \hat{r}}{r^2} & \mu_0 &= 4\pi \times 10^{-7} \text{ T} \cdot \text{m} / \text{A} \\ &= \frac{\mu_0}{4\pi} \frac{(6 \times 10^{-6} \text{ C})(8 \times 10^6 \frac{\text{m}}{\text{s}} \hat{j}) \times \hat{i}}{(0.5\text{m})^2} \\ &= -1.9 \times 10^{-5} \text{ T } \hat{k}\end{aligned}$$

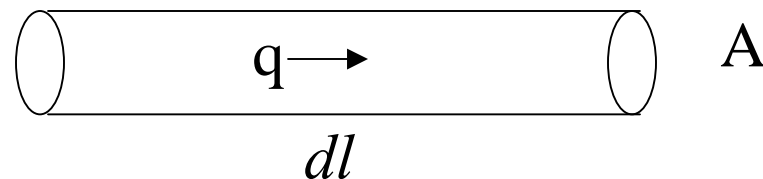
B) $x=0\text{m}, y=0.5, z=0\text{m}$

$$\vec{B} = 0 \quad \text{since}$$

\vec{v} and \hat{r} parallel.

Magnetic Fields from a current element

Suppose we have a current element of length dl , cross sectional area A and particle density n , #charges/volume. The total charge, dQ is



$dQ = n q A dl$. And recall that current is $I = n q v A$. The B field becomes,

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{dQ \vec{v} \times \hat{r}}{r^2} = \frac{\mu_0}{4\pi} n q A \frac{\vec{v} \times \hat{r}}{r^2} = \frac{\mu_0}{4\pi} \frac{I d\vec{l} \times \hat{r}}{r^2}$$

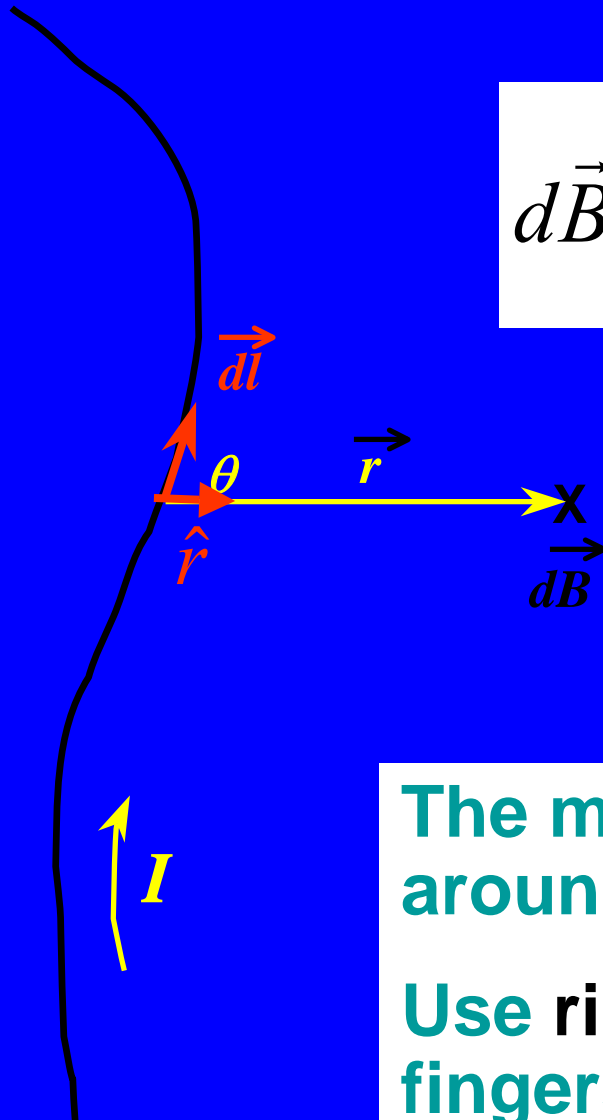
Vector, $d\vec{l}$, is the length of the current element in the direction of the current flow. This is called the **Biot-Savart Law**

Since n above is very large, a current (element) will give a much bigger magnetic field than that of a single charge.

Biot-Savart Law

$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{l} \times \hat{r}}{r^2}$$

$$\mu_0 = 4\pi \times 10^{-7} \frac{\text{N}}{\text{A}^2}$$



The magnetic field “circulates” around the wire

Use right-hand rule: thumb along I , fingers curl in direction of B .

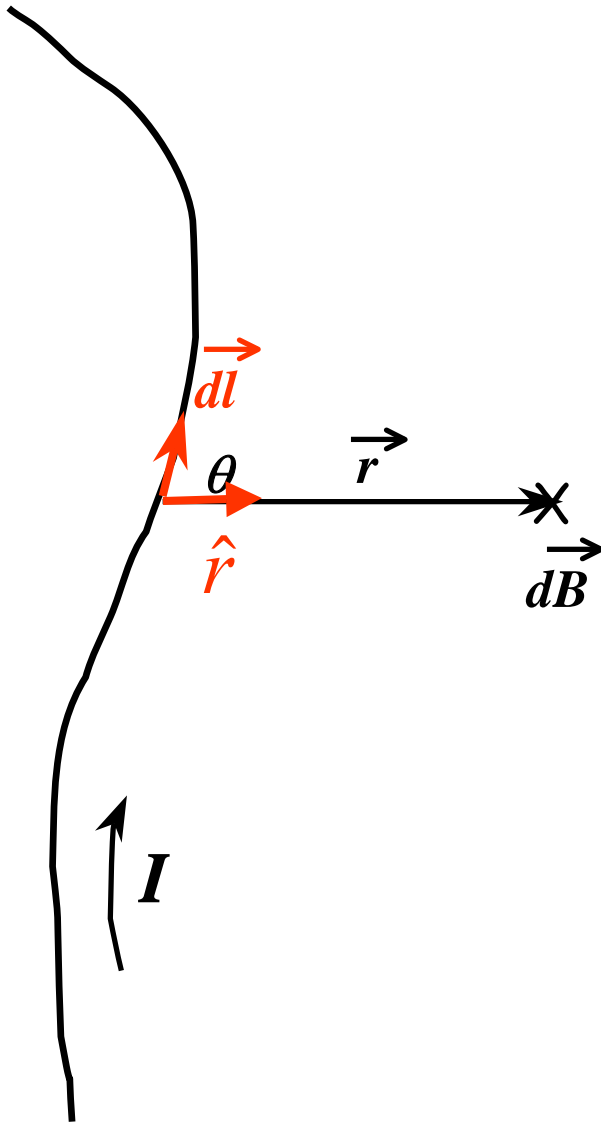
Magnetic Fields from a arbitrary wire

If we have an arbitrary wire with current I flowing, and we wish to get the B at a specific point from the entire wire, we integrate the formula

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{Id\vec{l} \times \hat{r}}{r^2}$$

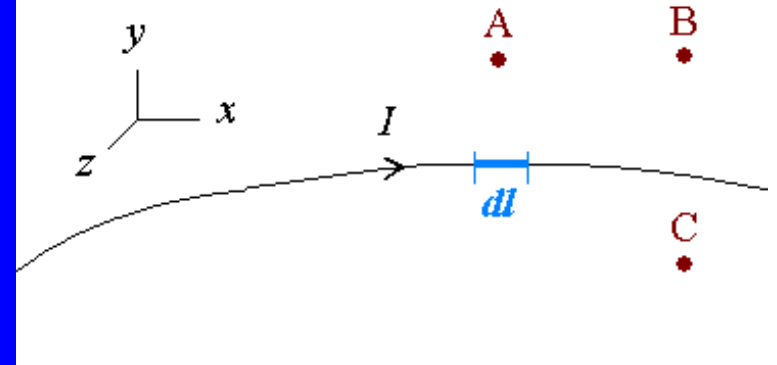
and obtain a line integral of a cross product

$$\vec{B} = I \frac{\mu_0}{4\pi} \int \frac{d\vec{l} \times \hat{r}}{r^2}$$



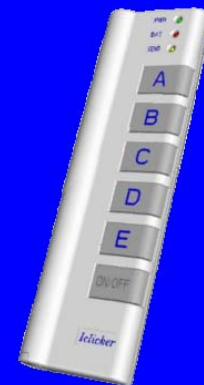
Question 1:

A current carrying wire (with no remarkable symmetry) is oriented in the x - y plane. Points A,B, & C lie in the same plane as the wire. The z -axis points out of the screen.



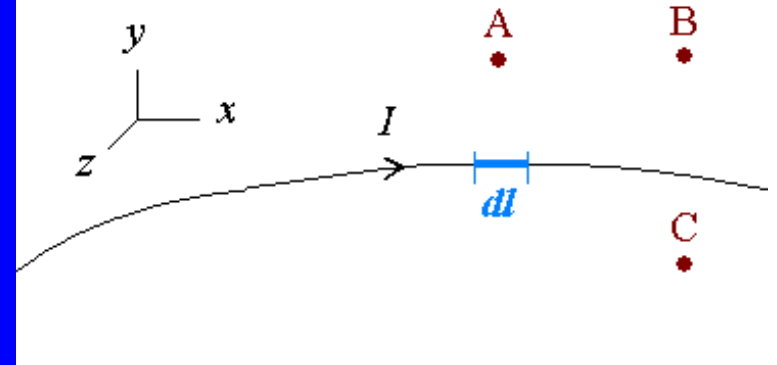
What direction is the magnetic field contribution from the segment dl at point A?

- | | | | | |
|------|------|------|------|------|
| A) | B) | C) | D) | E) |
| $+x$ | $-x$ | $+y$ | $+z$ | $-z$ |



Question 1:

A current carrying wire (with no remarkable symmetry) is oriented in the x - y plane. Points A, B, & C lie in the same plane as the wire. The z -axis points out of the screen.

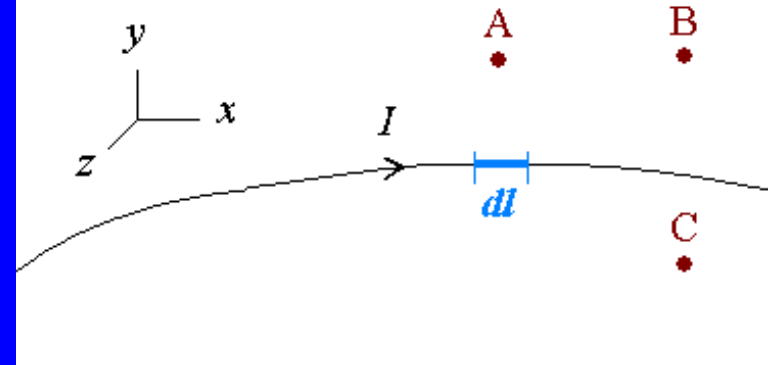


What direction is the magnetic field contribution from the segment dl at point A?

- | | | | | |
|------|------|------|------|------|
| A) | B) | C) | D) | E) |
| $+x$ | $-x$ | $+y$ | $+z$ | $-z$ |

Question 2:

A current carrying wire (with no remarkable symmetry) is oriented in the x - y plane. Points A,B, & C lie in the same plane as the wire. The z -axis points out of the screen.



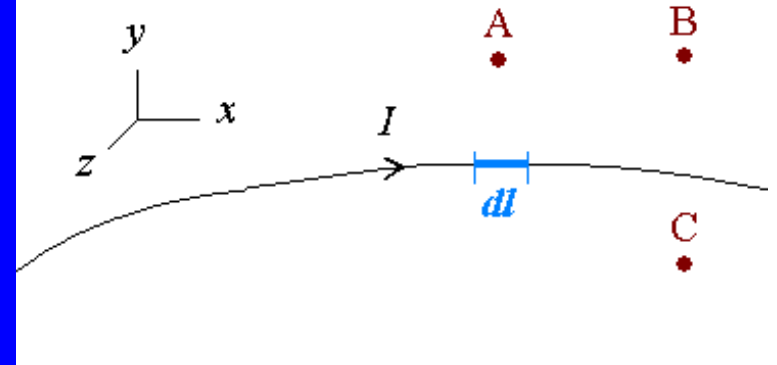
What direction is the magnetic field contribution from the segment dl at point B?

- | | | | | |
|------|------|------|------|------|
| A) | B) | C) | D) | E) |
| $+x$ | $-x$ | $+y$ | $+z$ | $-z$ |



Question 2:

A current carrying wire (with no remarkable symmetry) is oriented in the x - y plane. Points A, B, & C lie in the same plane as the wire. The z -axis points out of the screen.

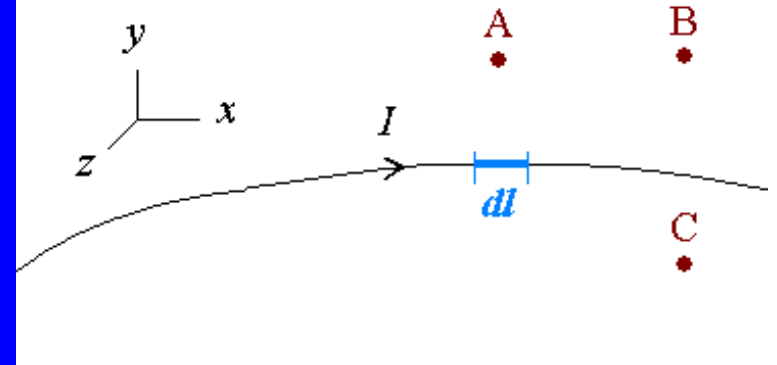


What direction is the magnetic field contribution from the segment dl at point B?

- | | | | | |
|------|------|------|------|------|
| A) | B) | C) | D) | E) |
| $+x$ | $-x$ | $+y$ | $+z$ | $-z$ |

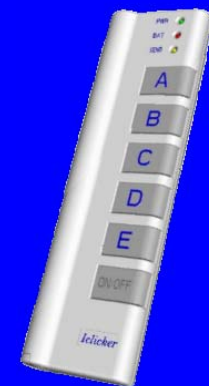
Question 3:

A current carrying wire (with no remarkable symmetry) is oriented in the x - y plane. Points A,B, & C lie in the same plane as the wire. The z -axis points out of the screen.



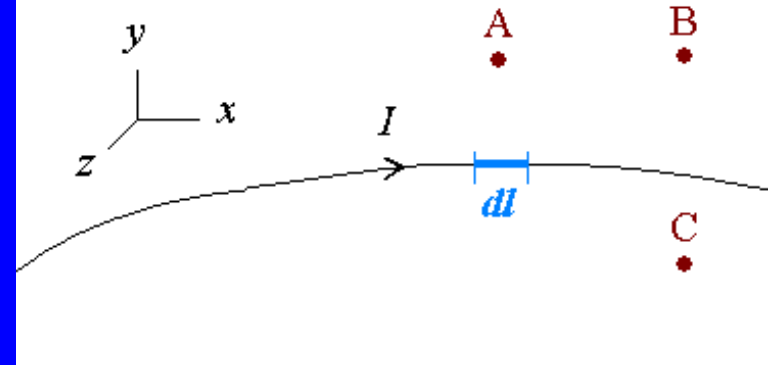
What direction is the magnetic field contribution from the segment dl at point C?

- | | | | | |
|------|------|------|------|------|
| A) | B) | C) | D) | E) |
| $+x$ | $-x$ | $+y$ | $+z$ | $-z$ |



Question 3:

A current carrying wire (with no remarkable symmetry) is oriented in the x - y plane. Points A, B, & C lie in the same plane as the wire. The z -axis points out of the screen.



What direction is the magnetic field contribution from the segment dl at point C?

A)

$+x$

B)

$-x$

C)

$+y$

D)

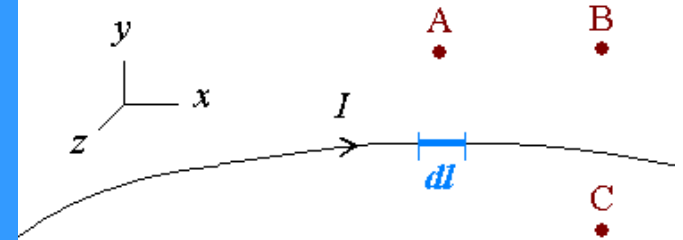
$+z$

E)

$-z$

dB points in the direction of $d\vec{l} \times \vec{r}$

$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{l} \times \vec{r}}{r^2}$$



A: dl is to the right, and r is up $\Rightarrow dB$ is out of the page

B: dl is to the right, and r is up and right $\Rightarrow dB$ is out of the page

C: dl is to the right, and r is down and right $\Rightarrow dB$ is into the page

Conclusion: at every point above the wire, dB is \odot . Below the wire, dB is \otimes

Check:

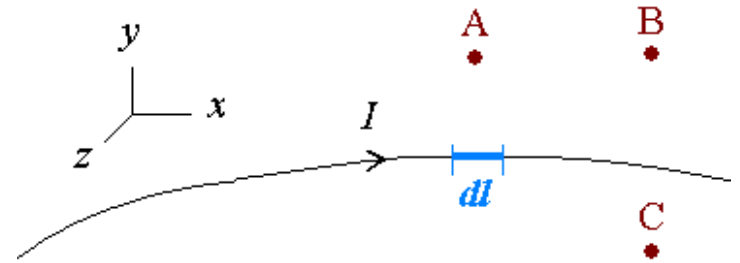
Would any of your answers for questions 1-3 change if we integrated dl over the whole wire?

NO.

Why or why not?

$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{l} \times \vec{r}}{r^2}$$

$d\vec{B}$ points in the direction of $d\vec{l} \times \vec{r}$



At point A: dl is to the right, and r is up $\Rightarrow d\vec{B}$ is out of the page

At point B: dl is to the right, and r is up and right $\Rightarrow d\vec{B}$ is out of the page

At point C: dl is to the right, and r is down and right $\Rightarrow d\vec{B}$ is into the page

For every point in the x - y plane and every piece of wire dl :

every dl and every r are always in the x - y plane

Since $d\vec{B}$ must be perpendicular to r and dl , $d\vec{B}$ is always in the $\pm z$ direction!

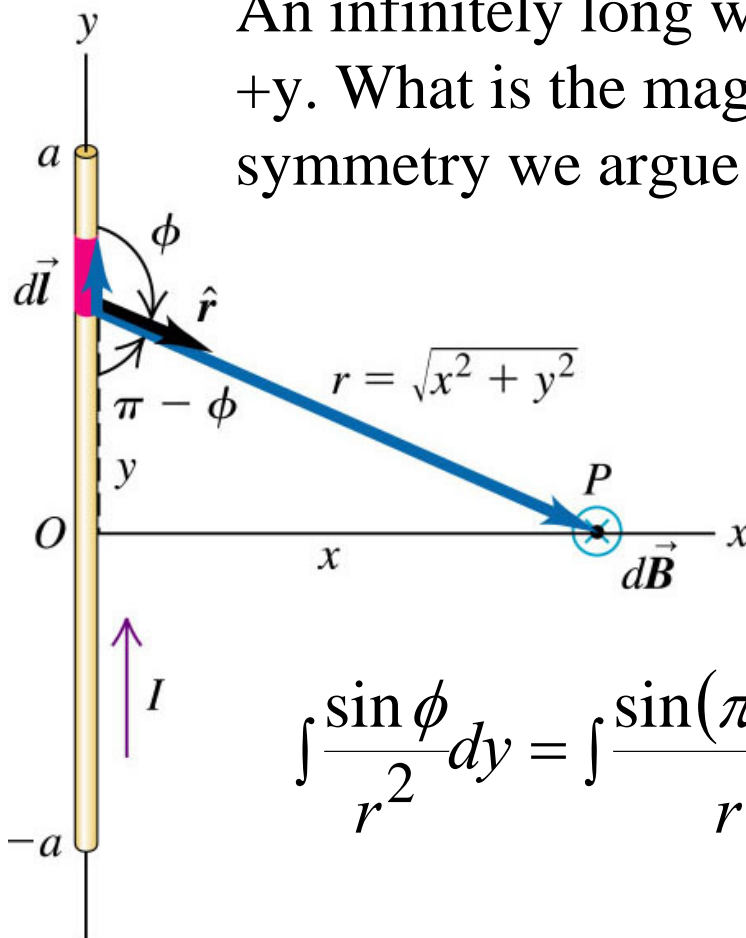
Conclusion:

At every point above the wire, the $d\vec{B}$ due to every piece dl is \odot .

Below the wire, the $d\vec{B}$ due to every piece dl is \otimes

Magnetic Fields from a long wire

An infinitely long wire along the y -axis with the current moving $+y$. What is the magnetic field at position x on the x -axis? By symmetry we argue the field must be in the $-z$ direction only.



$$\vec{B} = I \frac{\mu_0}{4\pi} \int \frac{d\vec{l} \times \hat{r}}{r^2} = I \frac{\mu_0}{4\pi} \int \frac{\sin \phi}{r^2} dl (-\hat{z})$$

$$= -\frac{\hat{z} I \mu_0}{4\pi} \int \frac{\sin \phi}{r^2} dy;$$

Since, $\sin(\phi) = \sin(\pi - \phi)$, we have

$$\int \frac{\sin \phi}{r^2} dy = \int \frac{\sin(\pi - \phi)}{r^2} dy = \int_{-\infty}^{+\infty} \frac{x}{r^3} dy = x \int_{-\infty}^{+\infty} \frac{1}{(y^2 + x^2)^{3/2}} dy$$

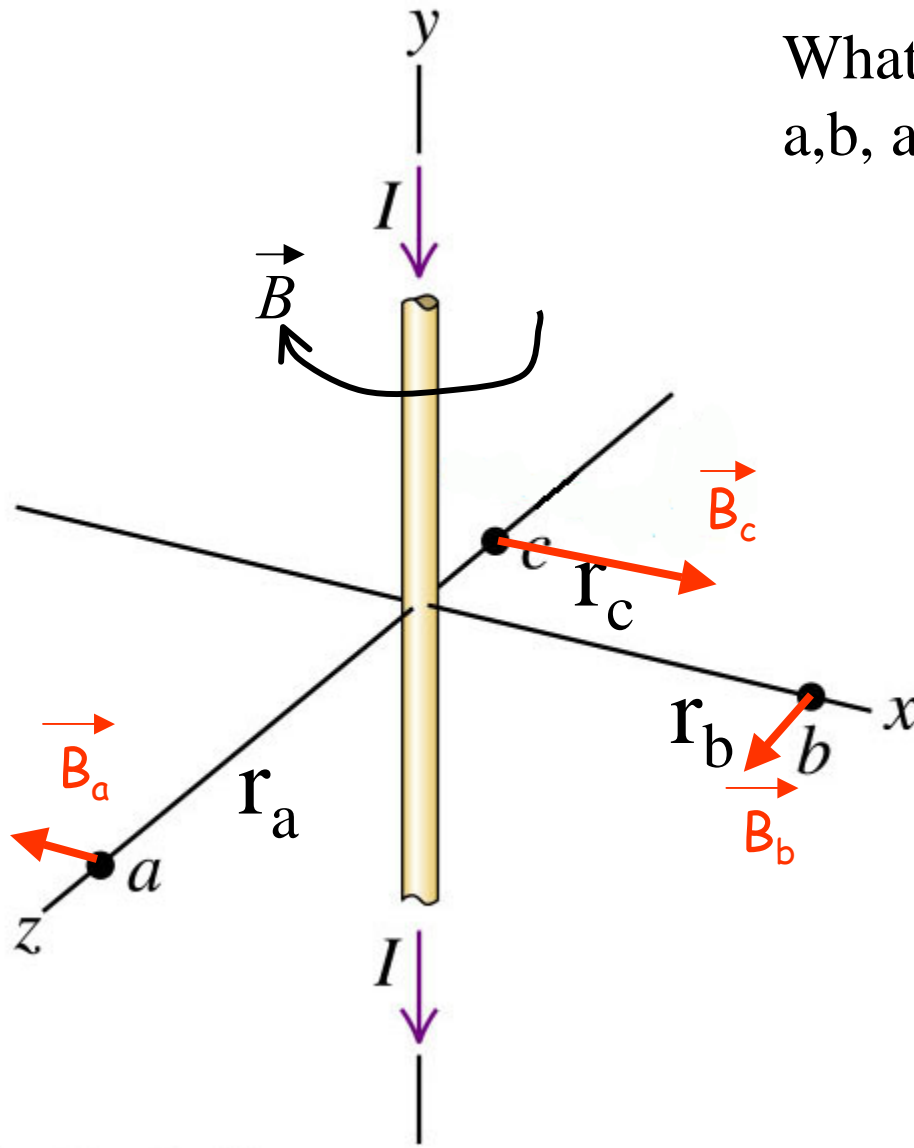
$$= x \left[\frac{1}{x^2} \frac{y}{\sqrt{y^2 + x^2}} \right]_{-\infty}^{+\infty} = \frac{2}{x}$$

$$\boxed{\vec{B} = \frac{\mu_0 I}{2\pi x} (-\hat{z})}$$

Magnetic Fields from a long wire

What are the magnetic fields at points a, b, and c?

$$|\vec{B}| = \frac{\mu_0 I}{2\pi r}$$



Into the 2nd half

- HW #8 → need magnetic equivalent of Gauss' Law
- Office Hours immediately after this class
(9:30 - 10:00) in WAT214 (1:30-2/1-1:30 M/WF)
- Last day to drop soon - grade feedback on webpage

